

$$\alpha, C \in R, a \in R_+, a \neq 1$$

$f(x)$	$\int f(x) dx$
0	C
1	$x + C$
x^α	$\frac{x^{\alpha+1}}{\alpha+1} + C, \quad \alpha \neq -1$
$\frac{1}{x}$	$\ln x + C$
e^x	$e^x + C$
a^x	$\frac{a^x}{\ln a} + C$

$f(x)$	$\int f(x) dx$
$\sin x$	$-\cos x + C$
$\cos x$	$\sin x + C$
$\frac{1}{\cos^2 x}$	$\operatorname{tg} x + C$
$\frac{1}{\sin^2 x}$	$-\operatorname{ctg} x + C$
$\frac{1}{1+x^2}$	$\operatorname{arc} \operatorname{tg} x + C = -\operatorname{arc} \operatorname{ctg} x + C$
$\frac{1}{\sqrt{1-x^2}}$	$\operatorname{arc} \sin x + C = -\operatorname{arc} \cos x + C$

Jeżeli $\int f(x) dx = F(x) + C$, to $\int f(ax + b) dx = \frac{1}{a} \cdot F(ax + b) + C, \quad a \neq 0$

$$\int \frac{f'(x)}{f(x)} dx = \ln|f(x)| + C$$

$$\int \frac{1}{a^2 + x^2} dx = \frac{1}{a} \cdot \operatorname{arc} \operatorname{tg} \left(\frac{x}{a} \right) + C, \quad a \neq 0$$

$$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \operatorname{arc} \sin \left(\frac{x}{a} \right) + C, \quad a > 0$$

Liniowość całki

$$\int f(x) \pm g(x) dx = \int f(x) dx \pm \int g(x) dx$$

$$\int a \cdot f(x) dx = a \cdot \int f(x) dx, \quad a \in R$$

Całkowanie przez części

$$\int u(x) \cdot v'(x) dx = \left. \begin{array}{l} u(x) \\ u'(x) \end{array} \right\} \begin{array}{l} v(x) \\ v'(x) \end{array} = u(x) \cdot v(x) - \int u'(x) \cdot v(x) dx$$

Całkowanie przez podstawienie, ($F'(x) = f(x)$)

$$\int \underbrace{f(g(x))}_{f(u)} \cdot \underbrace{g'(x) dx}_{du} = \int f(u) du = F(u) + C = F(g(x)) + C$$